

## STUDY OF AN INTERMEDIATE AGE OPEN CLUSTER IC 1434 USING GROUND-BASED IMAGING AND GAIA DR2 ASTROMETRY

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### ABSTRACT

We present a detailed photometric and kinematical analysis of the poorly studied open cluster IC 1434 using CCD VRI, APASS, and Gaia DR2 database for the first time. By determining the membership probability of stars we identify the 238 most probable members with a probability higher than 60% by using proper motion and parallax data as taken from the Gaia DR2 catalog. The mean proper motion of the cluster is obtained as  $\mu_x = -3.89 \pm 0.19$  and  $\mu_y = -3.34 \pm 0.19$  mas yr<sup>-1</sup> in both the directions of right ascension and declination. The radial distribution of member stars provides the cluster extent as 7.6 arcmin. We estimate the interstellar reddening  $E(B - V)$  as 0.34 mag using the transformation equations from the literature. We obtain the values of cluster age and distance as  $631 \pm 73$  Myr and  $3.2 \pm 0.1$  kpc.

### RESUMEN

Presentamos un estudio fotométrico y cinemático detallado del cúmulo IC 1434 utilizando por primera vez CCD VRI, APASS, y la base de datos Gaia DR2. Mediante el análisis de los movimientos propios y las paralajes del catálogo Gaia DR2 identificamos los 238 miembros más probables del cúmulo, con una probabilidad mayor que 60%. Encontramos que el movimiento propio medio del cúmulo es  $\mu_x = -3.89 \pm 0.19$  and  $\mu_y = -3.34 \pm 0.19$  mas yr<sup>-1</sup> en ascensión recta y declinación. La distribución radial de las estrellas miembros muestra que la extensión del cúmulo es 7.6 minutos de arco. Estimamos un enrojecimiento interestelar de  $E(B - V) = 0.34$  mag mediante las ecuaciones de transformación de la literatura. Obtuvimos una edad para el cúmulo de  $631 \pm 73$  millones de años y una distancia de  $3.2 \pm 0.1$  kpc.

*Key Words:* astrometry — Hertzsprung-Russell and colour-magnitude diagrams — open clusters and associations: individual: IC 1434

### 1. INTRODUCTION

Open clusters (OCs) are important tools to probe the Galactic disk properties (see, e.g., Friel 1995). OCs are very advantageous to interpret many queries regarding the assessment of chemical abundance gradients in the disk (see, e.g., Twarog, Ashman & Anthony-Twarog 1997; Chen, Hou & Wang 2003), Galactic structure and evolution (e.g., Janes & Adler 1982; Janes & Phelps 1994), interactions between thin and thick disks (e.g., Sandage 1988), as well as

the theories of stellar formation and evolution (e.g., Meynet, Mermilliod & Maeder 1993; Phelps & Janes 1993). It's not an easy task to segregate cluster members from field stars considering that OCs are generally projected against the Galactic disc stars. The second data release (DR2) (Gaia Collaboration et al. 2016a) contains 1.7 billion sources and was made public on 2018 April 24 (Jordi et al. 2010; Gaia Collaboration et al. 2016a,b; Salgado et al. 2017). The Gaia DR2 data contains photometric magnitudes in three bands ( $G$ ,  $G_{BP}$ , and  $G_{RP}$ ) and astrometric data at the sub-milliarcsecond level along with the parallax (Gaia Collaboration et al. 2018a). Gaia data have been used recently by many authors to

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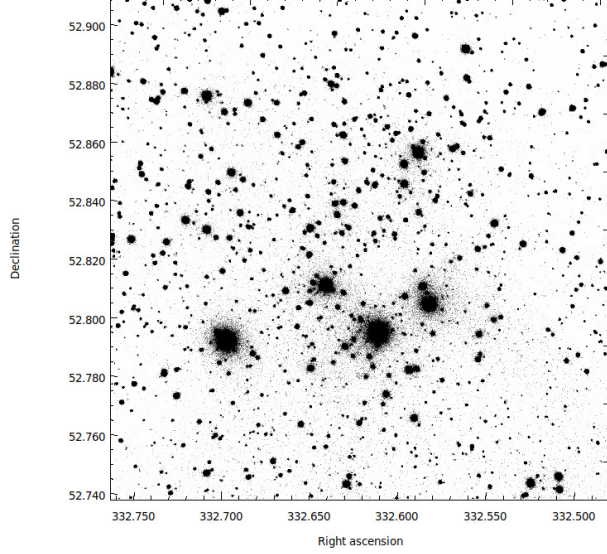


Fig. 1. Finding chart of the stars in the field of IC 1434. Filled circles of different sizes represent the brightness of the stars. The smallest size denotes stars of  $V \approx 20$  mag.

estimate the membership probability of stars lying towards the cluster regions (Cantat-Gaudin et al. 2018; Gao 2018; Rangwal et al. 2019; Bisht et al. (2019, 2020a, 2020b)).

The open cluster IC 1434 ( $\alpha_{2000} = 22^h 10^m 30^s$ ,  $\delta_{2000} = 52^\circ 50' 00''$ ;  $l=99^\circ.937$ ,  $b=-2^\circ.700$ ) is located in the second Galactic quadrant. Tadross (2009) analyzed this object using 2MASS and NOMAD data sets. He obtained the age, the interstellar reddening  $E(B-V)$ , and the distance of this object as 0.32 Gyr, 0.66 mag, and  $3035 \pm 140$  pc, respectively. In this paper, our main goal is to accomplish a deep and precise analysis of an intermediate-age open cluster IC 1434 using CCD  $VRI$ , APASS, and Gaia DR2 data.

The layout of the paper is as follows. A brief description of data used, data reduction, and calibration are described in § 2. § 3 deals with the study of proper motion and determination of membership probability of stars. The derivation of structural properties and of fundamental parameters using the most probable cluster members is carried out in § 4. The conclusions are presented in § 5.

## 2. OBSERVATIONS AND CALIBRATION OF CCD DATA

The  $VRI$  CCD photometric observations of IC 1434 were carried out using the 74-inch Kottamia astronomical observatory (KAO) of NRIAG in Egypt. Images were collected using a  $2k \times 2k$  CCD system. The observations were taken at the Newto-

TABLE 1

LOG OF OBSERVATIONS, WITH DATES AND EXPOSURE TIMES FOR EACH PASSBAND

Band	Exposure Time (seconds)	Date
<i>V</i>	120×3, 60×1	8 <sup>th</sup> November 2013
<i>R</i>	120×2, 60×1	"
<i>I</i>	120×3, 60×1	"

nian focus with a field area of  $10' \times 10'$  and a pixel scale of  $0''.305 \text{ pixel}^{-1}$  on 8<sup>th</sup> November 2013. The read-out noise was  $3.9 \text{ e}^-/\text{pixel}$ . Observations were organized in several short exposures with the air mass ranges of 1.32-1.62 in each of the filters, as described in Table 1. All CCD frames were observed with two amplifiers, which were treated for overscan, bias, and flat field corrections using an IRAF's code written by one of the authors (Y.H.M. Hendy, see Tadross et al. 2018). To perform the photometry, we used a DAOPHOT package on IRAF (Stetson 1987, 1992). The data reduction procedure was explained by Bisht et al. (2019). The identification chart for IC 1434 based on our  $V$ -band observations is shown in Figure 1.

To obtain the instrumental magnitudes of stars in the observed field, we used the point spread function of Stetson (1987). We transformed the pixel coordinates (X and Y) into right ascension and declination using the astrometry website (<https://nova.astrometry.net/>).

To transform the  $VRI$  instrumental magnitudes into Johnson and Kron-Cousin standard magnitudes, we used the photometric data available in the  $V$ -band from Maciejewski & Niedzielski (2008) and in the  $RI$ -bands from the USNO-B1.0 catalog (Monet et al. 2003).

The transformation equations for converting the instrumental magnitude in to standard magnitude, are as follows:

$$\begin{aligned}
 V &= V_{ins} - (0.14 \pm 0.039)(V - R) + 21.18 \pm 0.031, \\
 V - R &= (1.06 \pm 0.035)(V - R)_{ins} + 0.56 \pm 0.022, \\
 V - I &= (0.90 \pm 0.036)(V - I)_{ins} + 0.85 \pm 0.027.
 \end{aligned}$$

The respective errors in zero points and color coefficients are  $\approx 0.03$  mag shown in the above transformation equations. The internal errors derived from DAOPHOT are plotted against  $V$  magnitude in Figure 2. This figure shows that the average photometric errors are  $\leq 0.02$  mag at  $V \approx 18^{\text{th}}$  mag, and  $\leq 0.1$  mag at  $V \approx 19^{\text{th}}$  mag.

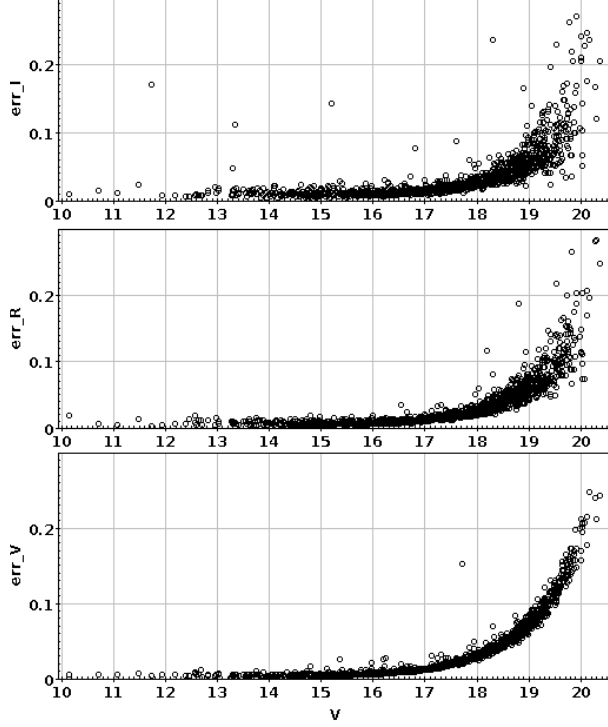


Fig. 2. Photometric errors in the  $V$ ,  $R$ , and  $I$  bands against  $V$  magnitude.

To compare the photometry, we have cross-identified the stars in our observed data with the American Association of Variable Star Observers (AAVSO) Photometric All-Sky Survey (APASS) DR9 catalog. We have assumed that stars are accurately matched if the difference in position is less than 1 arcsec and, in this way, we have found 32 common stars. The APASS survey is cataloged in five filters  $B$ ,  $V$ ,  $g$ ,  $r$ , and  $i$ . The range of magnitude in the  $V$  band is from 7 to 17 mag (Heden & Munari 2014). The DR9 catalog covers almost about 99 % of the sky (Heden et al. 2016). To obtain the Cousins  $I$  band using the Sloan  $ri$  photometric bands from the APASS catalog ( $I_{APASS} = i - (0.337 \pm 0.191)(r - i) - (0.370 \pm 0.041)$ ), we have adopted the method given by Tadross & Hendy (2016).

The difference indicates that present  $V$  and  $(V - I)$  measurements are in fair agreement with those of stars given in the APASS catalog. The comparable difference is found as 0.07 in the  $V$  band and 0.08 in  $(V - I)$  as shown in Figure 3.

### 2.1. Gaia DR2

The Gaia DR2 (Gaia Collaboration et al. 2018b) database within a  $20'$  radius of the cluster is used for the astrometric analysis. These data consist of

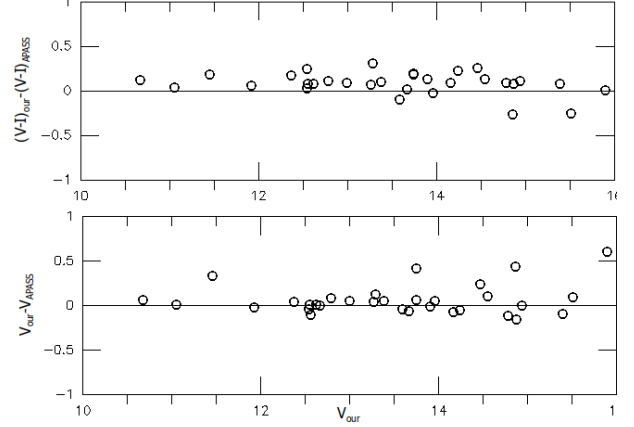


Fig. 3. Differences between measurements presented in the APASS catalog and this study for the  $V$  magnitude and  $(V - I)$  colors. A zero difference is indicated by the solid line.

positions on the sky ( $\alpha, \delta$ ), parallaxes and proper motions ( $\mu_\alpha \cos \delta, \mu_\delta$ ) with a limiting magnitude of  $G = 21$  mag. The errors in photometric magnitudes ( $G$ ,  $G_{BP}$ , and  $G_{RP}$ ) versus  $G$  mag are shown in Figure 4. In this figure, we find the mean errors in the  $G$  band are  $\approx 0.01$  mag while the mean errors in the  $G_{BP}$  and  $G_{RP}$  bands are  $\approx 0.1$  mag at 20 mag. The proper motions with their respective errors are plotted against  $G$  magnitude in Figure 5. The uncertainties in the corresponding proper motion components are  $\approx 0.06$  mas yr $^{-1}$  (for  $G \leq 15$  mag),  $\approx 0.2$  mas yr $^{-1}$  (for  $G \approx 17$  mag), and  $\approx 1.2$  mas yr $^{-1}$  (for  $G \approx 20$  mag).

### 3. PROPER MOTION STUDY AND MEMBERSHIP PROBABILITIES OF STARS

The proper motion of a cluster is a change in its angular position with time as seen from the center of mass of the Solar System. Proper motions play an influential role to eliminate non-members from the cluster's main sequence (Yadav et al. 2013; Bisht et al. 2020a). We have cross-matched our observational data in  $VRI$  bands and data from the Gaia DR2 catalog. A circle of 0.6 mas/yr around the cluster center in the VPD characterizes our membership criteria as shown in Figure 6. The chosen radius in the VPD is a compromise between losing members with poor proper motions and including field stars.

The OCs are highly contaminated by a large number of foreground/background stars especially towards the fainter end of the main sequence. Vasilevskis et al. (1958) have set up a mathematical model to obtain membership probabilities of stars

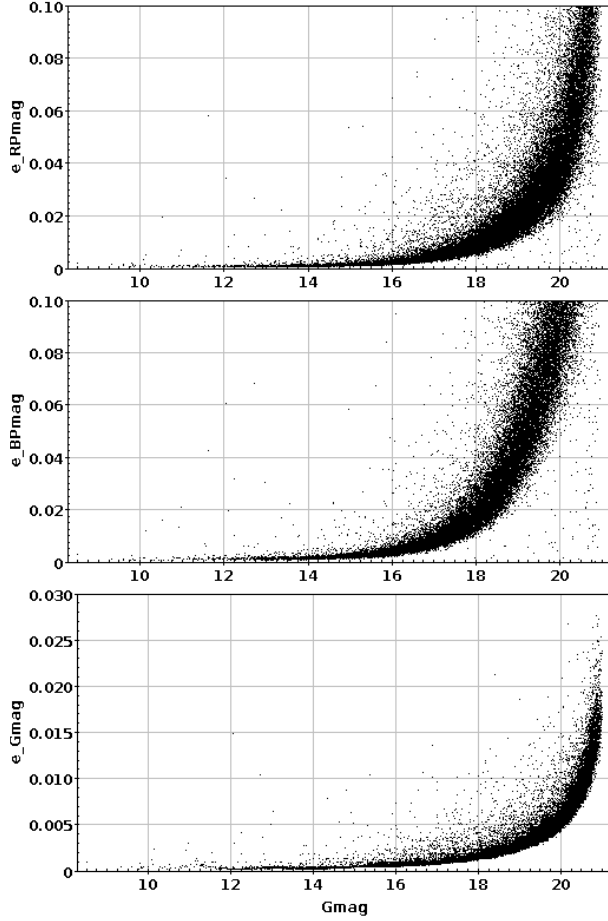


Fig. 4. Photometric errors in the Gaia bands ( $G$ ,  $BP$ , and  $RP$ ) against  $G$  magnitude.

using proper motion data. A revised technique was developed by Stetson (1980) and Zhao & He (1990) to check the membership of stars in OCs based on proper motions. To find the membership probability of stars towards the region of IC 1434, we have adopted the criteria of Kharchenko et al. (2004). This method has been previously used by Bisht et al. (2018) for OCs Teutsch 10 and Teutsch 25. Hendy (2018) used this method for the open cluster FSR 814. The kinematical probability of stars is expressed as:

$$P_k = e^{\left[ -0.25 \left( \frac{(\mu_x - \bar{\mu}_x)^2}{\sigma_x^2} + \frac{(\mu_y - \bar{\mu}_y)^2}{\sigma_y^2} \right) \right]},$$

where  $\sigma_x^2 = \sigma_{\mu_x}^2 + \sigma_{\bar{\mu}_x}^2$  and  $\sigma_y^2 = \sigma_{\mu_y}^2 + \sigma_{\bar{\mu}_y}^2$ . Here  $\mu_x$  and  $\mu_y$  are the proper motion of a particular star, while  $\sigma_{\mu_x}$  and  $\sigma_{\mu_y}$  are the corresponding errors. The  $\bar{\mu}_x$  and  $\bar{\mu}_y$  are the mean values of the proper mo-

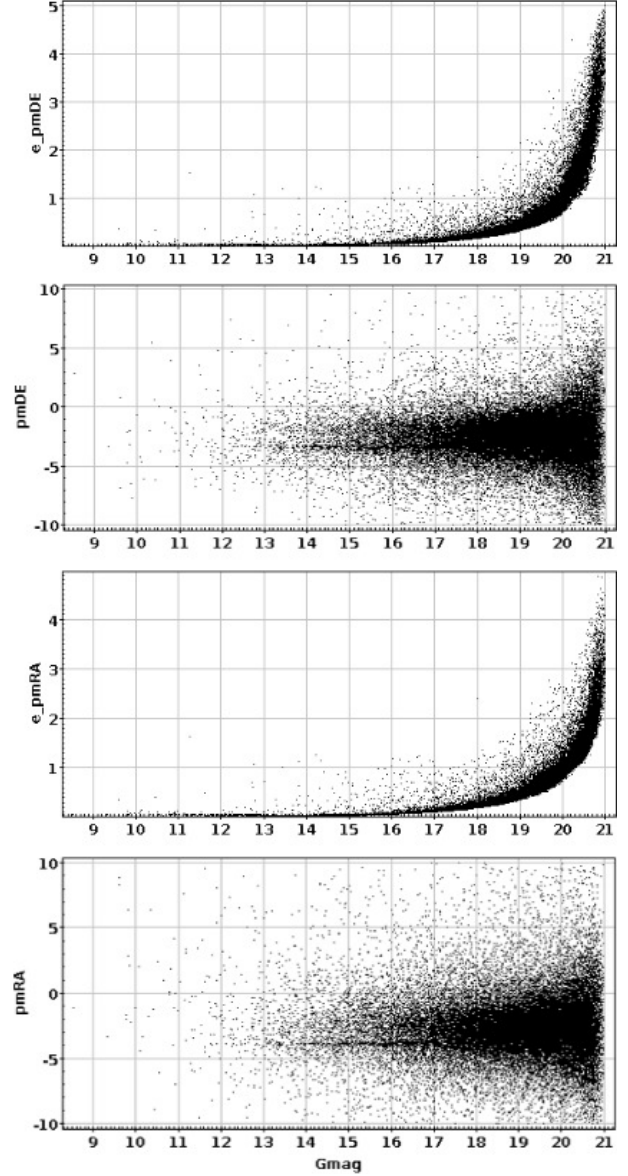


Fig. 5. Plot of proper motions and their errors versus  $G$  magnitude.

tions, while  $\sigma_{\bar{\mu}_x}$  and  $\sigma_{\bar{\mu}_y}$  are their corresponding standard deviations. Using the above method, we identified possible members of IC1434 if their membership probability was higher than 60% which can be seen in Figure 7.

We used only probable cluster members to estimate the mean value of proper motions and parallax of IC 1434. We fitted Gaussian profile to the constructed histograms shown in Figure 8. We obtained the mean-proper motion of IC 1434 as  $-3.89 \pm 0.19$  and  $-3.34 \pm 0.19$  mas yr $^{-1}$  in RA and DEC directions, respectively. We determined the mean value

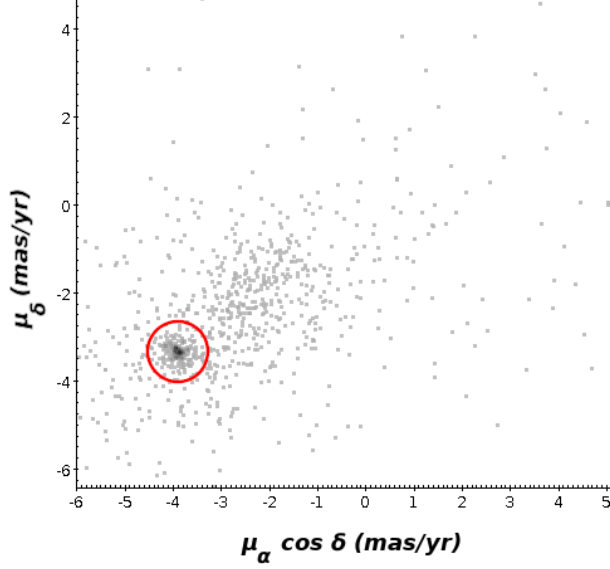


Fig. 6. Vector point diagram. The circle defines the cluster region of IC 1434 within a radius of 0.6 mas/yr. The color figure can be viewed online.

of the parallax as  $0.30 \pm 0.11$  mas. Our findings are very close to the values given by Cantat-Gaudin et al. (2018).

Finally, we considered a star as a most probable member if it lies within a 0.6 mas/yr radius in the VPD, having a membership probability higher than 60% and a parallax within  $3\sigma$  from the mean parallax of the cluster IC 1434. In Figure 9, we plot the proper motions and parallax distribution of the most probable members (denoted by red dots) and of all observed stars (denoted by gray dots) against  $G$  magnitude. In this figure, the horizontal solid line indicates the mean value of the proper motions and parallaxes.

#### 4. STRUCTURAL PROPERTIES OF IC 1434

##### 4.1. Spatial Structure: Radial Density Profile

The accuracy of the central coordinates is very important for the reliable estimation of the cluster's main fundamental parameters (e.g., age, distance, reddening, etc.). We applied a star-count technique to obtain the center coordinates towards the area of IC 1434. The resulting histograms in both the RA and DEC directions are shown in the left panel of Figure 10. The Gaussian curve-fitting at the central zones provided the center coordinates as  $\alpha = 332.612 \pm 0.06$  deg ( $22^h 10^m 26.8^s$ ) and  $\delta = 52.84 \pm 0.04$  deg ( $52^\circ 50' 24''$ ). These estimated values are in very good agreement with the values given by Dias et al. (2002) and Cantat-Gaudin et al. (2018).

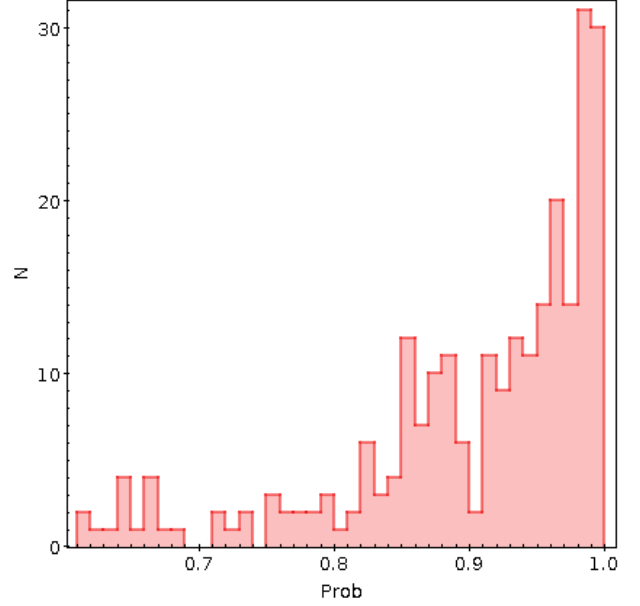


Fig. 7. Membership probability histogram of stars for IC 1434. We considered stars with a probability  $\geq 0.6$  as cluster members. The color figure can be viewed online.

TABLE 2

STRUCTURAL PARAMETERS OF IC 1434\*

Name	$f_0$	$f_b$	$R_c$	$c$	$\delta_c$
IC 1434	$23.70 \pm 3.49$	$8.78 \pm 0.21$	$1.25 \pm 0.19$	0.78	3.7

\*Background and central densities are given in units of stars per arcmin<sup>2</sup>. Core radius ( $r_c$ ) is given in arcmin.

The radial density profile (RDP) is plotted in Figure 11 to estimate the radius of the cluster. We divided the observed area of IC 1434 into several concentric rings. The number density,  $R_i$ , in the  $i^{th}$  zone is determined by using the formula  $R_i = \frac{N_i}{A_i}$ , where  $N_i$  is the number of stars and  $A_i$  is the area of the  $i^{th}$  zone. This RDP flattens at  $R \approx 7.6$  arcmin and begins to merge with the background density, as clearly shown in the right panel of Figure 11. Therefore, we consider 7.6 arcmin as the cluster radius. A smooth continuous line represents the fitted King (1962) profile:

$$f(r) = f_{bg} + \frac{f_0}{1 + (r/r_c)^2}$$

where  $r_c$ ,  $f_0$ , and  $f_{bg}$  are the core radius, central density, and the background density level, respectively. By fitting the King model to RDP, we estimated the structural parameters of IC 1434 and list them in Table 2.

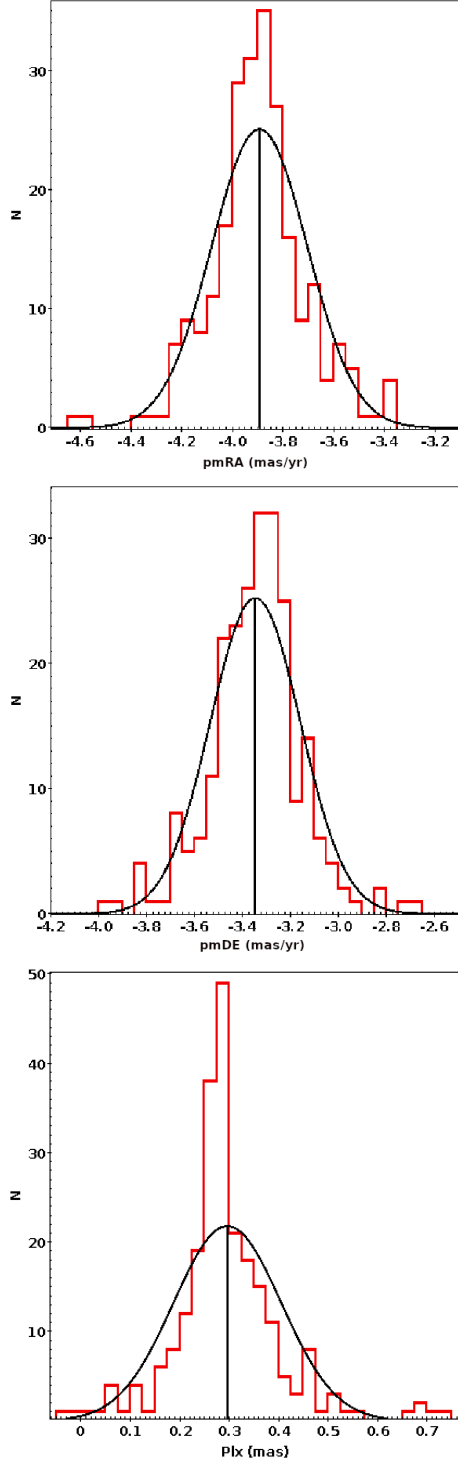


Fig. 8. Histogram to determine the mean values of proper motions in RA and DEC (top and middle panels). Histogram to find the mean parallax (bottom panel). The Gaussian function fits to the central bins provide the mean values in proper motion and parallax shown in each panel. The color figure can be viewed online.

We estimated the concentration parameter using equation  $c = \log\left(\frac{r_{lim}}{r_c}\right)$ , as given by Peterson & King (1975). In the present study, the concentration parameter was found to be 0.78 for IC 1434. Maciejewski & Niedzielski (2007) reported that  $R_{lim}$  may vary for individual clusters from  $2R_c$  to  $7R_c$ . The estimated value of  $R_{lim}$  ( $\approx 6.1R_c$ ) shows a fair agreement with the Maciejewski & Niedzielski (2007) value. We obtained the density contrast parameter ( $\delta_c = 1 + [f_0/f_{bg}]$ ) for IC 1434 as 3.7. It is lower than the range  $7 \leq \delta_c \leq 23$  derived by Bonatto & Bica (2009). This demonstrates that IC 1434 is a sparse cluster.

#### 4.2. Age and Distance Estimation Using the CMD

Age and distance are important parameters to trace the structure and chemical evolution of the Milky Way Galaxy using OCs (Friel & Janes 1993). The  $(G, BP - RP)$ , and  $(V, V - I)$  color magnitude diagrams (CMDs) are shown in Figure 12. In this figure, filled dots stand for the most probable cluster members with membership probability  $\geq 60\%$  while open circles stand for the ones matched with the catalog of Cantat-Gaudin et al. (2018). The age of IC 1434 was estimated by fitting the theoretical isochrones of Marigo et al. (2017) with a metallicity of  $Z = 0.0152$  to the CMDs, as shown in Figure 12. In this figure, we used the isochrones of different ages,  $\log(\text{age}) = 8.75, 8.80$  and  $8.85$ . We found the best global fit at  $\log(\text{age})=8.80$ , which corresponds to a cluster age of  $631 \pm 73$  Myr.

Our estimated value of the color-excess in the Gaia bands  $E(BP - RP)$  is 0.43 mag from the isochrone fitting to the CMD's. We calculated the interstellar reddening  $E(B - V)$  as 0.34 mag using the transformation equations ( $E(B - V) = 0.785 E(BP - RP)$ ) as taken from Abdelaziz et al. (2020). The distance modulus ( $m - M_G = 12.51$  mag) of IC 1434 provides the heliocentric distance as  $3.2 \pm 0.1$  kpc. Our estimated values of  $E(B - V)$  and distance modulus are in fair agreement with the values  $E(B - V) = 0.49$  and  $m - M_G = 12.43$  obtained by Angelo et al. (2020).

We obtained the Galactocentric distance as  $9.4 \pm 0.1$  kpc by assuming an  $8.3$  kpc distance of the Sun to the Galactic center. The Galactocentric coordinates are estimated as  $X_\odot = -0.55 \pm 0.04$  kpc,  $Y_\odot = 3.1 \pm 0.2$  kpc and  $Z_\odot = -0.15 \pm 0.010$  kpc. The estimated values of the Galactocentric coordinates are very close to the values obtained by Cantat-Gaudin et al. (2018).

We also checked the distance of IC 1434 using the parallax of stars from the Gaia DR2 cat-



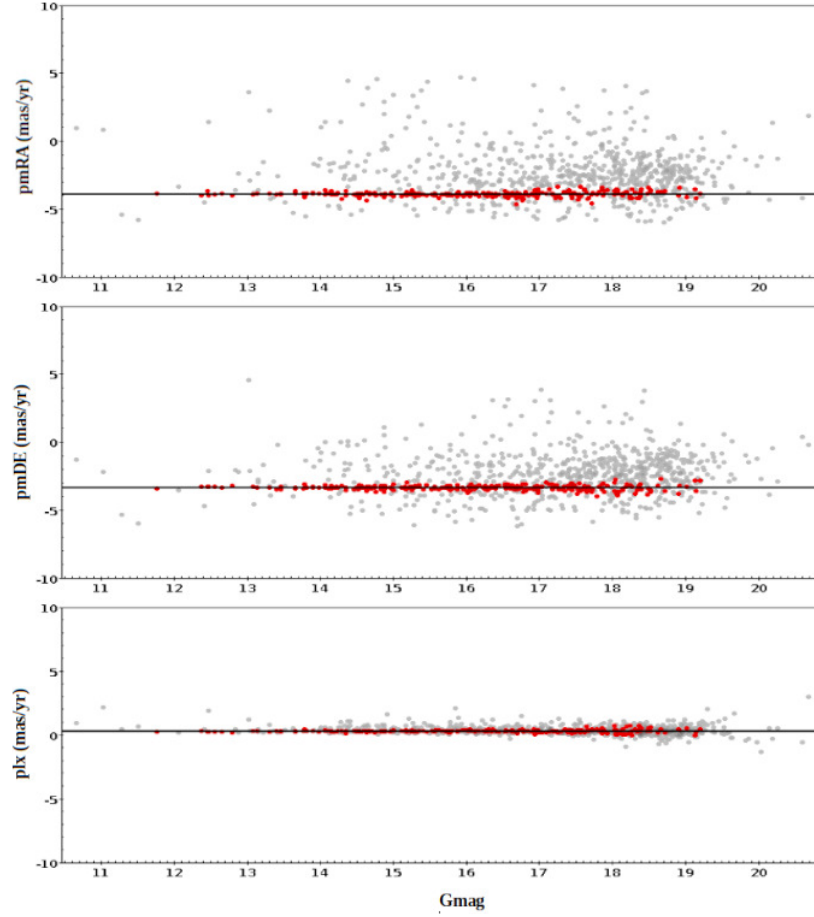


Fig. 9. Proper motion components and parallax distribution of most probable members (red dots) and all stars (gray dots) against  $G$  band magnitude. The horizontal line indicates the mean value of proper motion and parallax. The color figure can be viewed online.

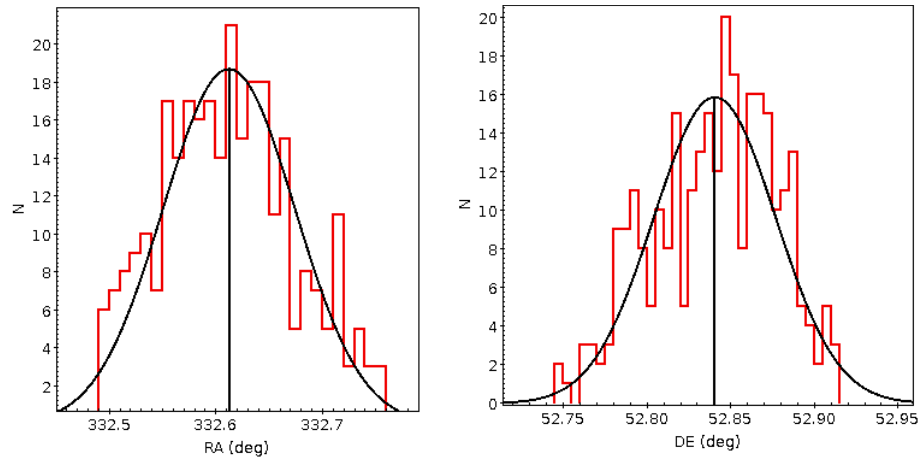


Fig. 10. Profiles of stellar counts across cluster IC 1434. Gaussian fits have been applied. The center of symmetry about the peaks of right ascension and declination is taken to be the position of the cluster center. The color figure can be viewed online.

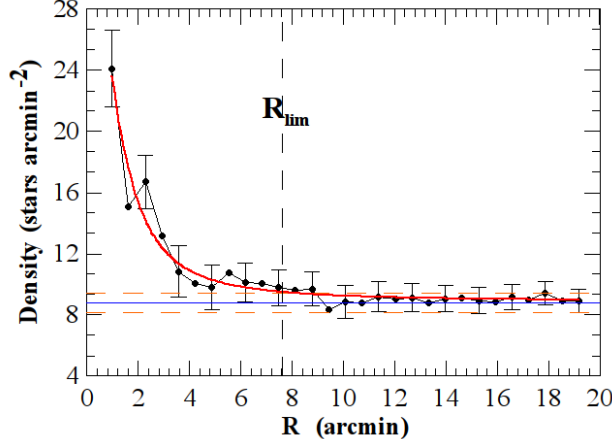


Fig. 11. Surface density distribution of the cluster IC 1434. Errors are determined from sampling statistics  $\frac{1}{\sqrt{N}}$ , where  $N$  is the number of stars used in the density estimation at that point. The smooth line represents the fitted profile whereas the dotted line shows the background density level. Long and short dash lines represent the errors in the background density. The color figure can be viewed online.

alog. We found the distance of this object to be 3.3 kpc, which is very close to our estimation from the isochrone fitting method. Angelo et al. (2020), Cantat-Gaudin (2020), Kharchenko et al. (2013), and Tadross (2009) have determined distance values for IC 1434 of 3.1, 3.3, 3.2, and 3.0 kpc, respectively. Our derived value of the distance is in good agreement with Angelo et al. (2020), Cantat-Gaudin (2020), and Kharchenko et al. (2013). The distance estimation of IC 1434 by Tadross (2009) is based on 2MASS and NOMAD data. Our obtained value of the distance is more precise than that of Tadross (2009) because our estimation is based on good quality optical data along with the high precision Gaia DR2 astrometry.

## 5. CONCLUSIONS

We presented a photometric and kinematic study of the poorly studied open cluster IC 1434 using CCD *VRI* and Gaia DR2 data. We estimated the membership probabilities of stars towards the region of IC 1434 and found 238 members with a membership probability  $\geq 60\%$ . We used those probable members to derive the fundamental parameters. The main results of the current investigation are as follows:

- The updated cluster center coordinates are estimated as:  $\alpha = 332.612 \pm 0.06$  deg ( $22^h 10^m 26.8^s$ ) and  $\delta = 52.84 \pm 0.04$  deg ( $52^\circ 50' 24''$ ) using the

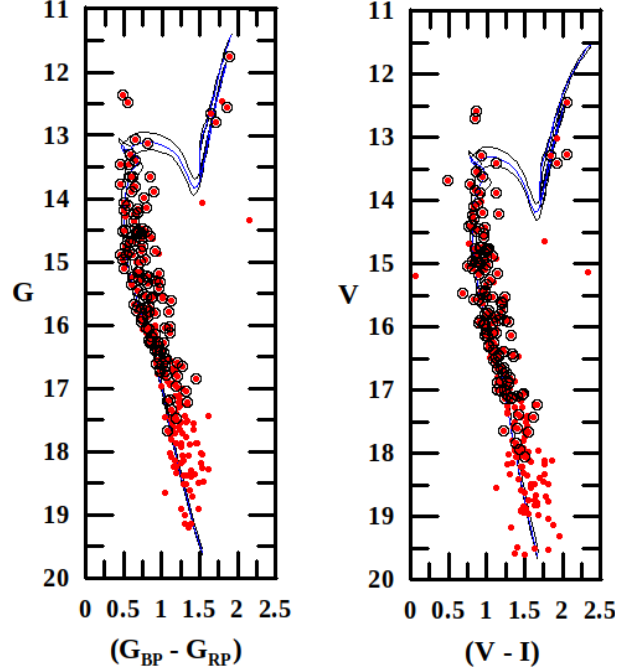


Fig. 12. Isochrone fitting to the CMDs. The curves are the solar metallicity isochrones taken from Marigo et al. (2017) for  $\log(\text{age}) = 8.75, 8.80$ , and  $8.85$ . The filled and open circles are our 238 members and the 127 members of Cantat-Gaudin et al. (2018), respectively. The color figure can be viewed online.

most probable cluster members. The cluster radius is obtained as 7.6 arcmin using the radial density profile.

- On the basis of the vector point diagram and membership probability estimation of stars, we identified 238 most probable cluster members for IC 1434. The mean PM of the cluster is estimated as  $-3.89 \pm 0.19$  and  $-3.34 \pm 0.19$  mas yr $^{-1}$  in the RA and DEC directions, respectively.
- The distance to the cluster IC 1434 is determined as  $3.2 \pm 0.1$  kpc. This value is well supported by the distance estimated using the mean parallax, 3.3 kpc. The age is estimated as  $631 \pm 73$  Myr by comparing the cluster CMD with the theoretical isochrone given by Marigo et al. (2017) with  $Z = 0.0152$ .

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