# EFFECTS OF MAGNETIC TURBULENCE ON THE DYNAMICS OF PICKUP IONS IN THE IONOSHEATH OF MARS 

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#### Abstract

RESUMEN Se estudian los efectos que las fluctuaciones magnéticas turbulentas tienen sobre la dinámica de iones pickup de $\mathrm{O}^{+}$en las regiones polares magnéticas de la ionofunda de Marte. En particular estudiamos su efecto en los perfiles de velocidad promedio como función de la altitud sobre los polos, con el fin de comparar con datos reciente del Mars Express que indican que su velocidad promedio es pequeña y esencialmente en la dirección antisolar. Se encuentra que, aunque las fluctuaciones magnéticas ocasionan desviaciones del simple movimiento de arrastre girotrópico, incluso amplitudes de fluctuación más grandes que las medidas no son capaces de reproducir los perfiles verticales de velocidad de los iones de $\mathrm{O}^{+}$. Concluímos que otro mecanismo físico, diferente a uno puramente de dinámica de partículas cargadas, está actuando sobre estos iones en el terminador marciano. Una posibilidad es que exista una interacción de tipo viscoso entre el viento solar y la ionosfera marciana a bajas altitudes.


#### Abstract

We study some of the effects that magnetic turbulent fluctuations have on the dynamics of pickup $\mathrm{O}^{+}$ions in the magnetic polar regions of the Mars ionosheath. In particular we study their effect on the bulk velocity profiles of ions as a function of altitude over the magnetic poles, in order to compare them with recent Mars Express data; that indicate that their average velocity is very low and essentially in the anti-sunward direction. We find that, while magnetic field fluctuations do give rise to deviations from simple $\mathbf{E} \times \mathbf{B}$-drift gyromotion, even fluctuation amplitudes much greater than those of in situ measurements are not able to reproduce the vertical velocity profile of $\mathrm{O}^{+}$ions. We conclude that other physical mechanisms, different from a pure charged particle dynamics, are acting on pickup ions at the Martian terminator. One possibility is a viscous-like interaction between the Solar Wind and the Martian ionosphere at low altitudes.


Key Words: acceleration of particles — magnetic fields - methods: numerical planets and satellites: individual (Mars) - turbulence

## 1. INTRODUCTION

The interaction of the solar wind (SW) with Solar System objects with a negligle intrinsic magnetic field and an atmosphere (e.g., Venus and Mars) is currently being investigated by several space missions (e.g., Venus and Mars Express), that will enhance our understanding of plasma interaction processes in such environments (e.g., Ma et al. 2008). In particular, a comparison of different models for the

[^0]global interaction of the solar wind, a weakly collisional plasma (e.g., Marsh 1994; Echim, Lemaire, \& Lie-Svendsen 2011), with Mars has been done by Brain et al. (2010) who included MHD, multifluid and hybrid models. All these models, as well as the gasdynamic convected magnetic field models (e.g., Belotserkovskii et al. 1987; Spreiter \& Stahara 1994), have greatly advanced our knowledge of the complex interaction of the SW plasma and the Martian ionosphere.

An important component of the Martian plasma environment, especially at low and mid altitudes, is
the population of oxygen ions $\left(\mathrm{O}^{+}\right)$produced by the UV solar radiation and charge exchange reactions. These are picked up by the SW convective electric field and removed from the planet, in turn affecting the solar wind interaction with Mars (e.g., Ledvina, Ma, \& Kallio 2008; Withers 2009).

Recently, Pérez-de-Tejada et al. (2009; hereafter PdT09) have pointed out that the analysis of Mars-Express measurements, conducted with the ASPERA-3 instrument (Barabash et al. 2006), indicates that the bulk velocity of $\mathrm{O}^{+}$ions, presumably of ionospheric origin, as they stream at low altitude over the magnetic poles of the planet is mostly in the anti-sunward direction (see Figure 1). This result is unexpected in the context of a SW-ionosphere interaction in which the acceleration of pickup ions is essentially due to the action of the convective electric field, E. As shown in Reyes-Ruiz, Aceves, \& Pérez-de-Tejada (2010, hereafter RAP10), in the context of a simplified model for the geometry of the IMF and SW flow in the ionosheath of Mars, the bulk velocity of pickup $\mathrm{O}^{+}$ions in gyromotion, as they pass over the magnetic poles of the planet, is strongly dominated by the vertical component ( $v_{z}$, normal to the plane of the ecliptic).

A qualitatively similar conclusion can also be reached from the results of MHD simulations using more complicated IMF and Martian magnetic field models to study the dynamics of heavy ions in the region (e.g., Fang et al. 2008), and seen in earlier $\mathrm{O}^{+}$pickup ion trajectories in a draped magnetic field model (e.g., Luhmann \& Schwingenschuh 1990; Luhmann 1990; Lichtenegger et al. 2000). In RAP10 it is argued that a largely horizontal bulk velocity of $\mathrm{O}^{+}$ ions can be explained in terms of a viscous-like interaction between the SW and ionospheric plasmas, as found in the numerical simulations of Reyes-Ruiz et al. (2010, hereafter RPAV10).

It has been suggested that magnetic field fluctuations, known to be widespread in the ionosheath of Mars and other non-magnetic bodies (Tsurutani, Glassmeier, \& Neubauer 1995; Nagy et al. 2004; Grebowsky et al. 2004; Espley et al. 2004; Vörös et al. 2008), may be responsible for modifying the gyromotion of pickup ions, enhancing pitch-angle scattering and ion heating and acceleration (e.g., Wang, Wu, \& Yoon 2006, and references therein). Najib et al. (2011) have noted more recently that the presence of wave activity and turbulence leads to waveparticle interactions that resemble collisions, hence probably modifying the ion distribution function. In this paper we study the possibility that such modifications of simple gyromotion due to turbulence-like


Fig. 1. ASPERA-3 in situ measurements of the velocities profiles of SW protons (top) and $\mathrm{O}^{+}$pickup ions (bottom) over the terminator of Mars; coordinates are in a MSE system, and the data is taken from PdT09. Four altitudes of the spacecraft are indicated as dotted vertical lines. The dominance of the $x$-component of the velocity of $\mathrm{O}^{+}$ions over its $z$ component is very clear, contrary to what is expected from a pure $\mathbf{U} \times \mathbf{B}$-drift.
fluctuations of the magnetic field, in the ionosheath over the magnetic poles of Mars lead to a bulk velocity profile for $\mathrm{O}^{+}$ions as that reported by PdT09 from the ASPERA-3 measurements.

It is worth emphasizing that global MHD or hybrid simulations analyzing the motion of ionospheric ions (Nagy et al. 2004; Fang et al. 2008; Brain et al. 2010; Kallio et al. 2010; Najib et al. 2011, and the review by Nagy et al. 2004) do not include the effect of small-scale turbulent fluctuations of the magnetic field, known to exist in the ionosheath of nonmagnetic Solar System bodies. These models essentially use the B field obtained directly from MHD simulations to follow the dynamics of the $\mathrm{O}^{+}$ions. Hence, our approach does not physically model the same phenomena that the above models are able to investigate. On other hand, our model does not consider the effect that the crustal field (e.g., Acu na et al. 1998; Zhang \& Li 2009) can have on the ion dynamics.

This paper is organized as follows. In § 2 we present the basic equations and methodology used for our analysis, including the prescription for constructing the turbulent magnetic fields employed


Fig. 2. Configuration used to study the motion of pickup ions, of mass $m$ and charge $q$. The $X$-axis points toward the Sun, the $Z$-axis points perpendicular to the ecliptic and the $Y$-axis completes a right-hand triad. The draped magnetic field around Mars goes from a minimum to a maximum at the equator and pole, respectively. The SW velocity rises from a minimum to a maximum at the equator and pole, respectively. The angle $\theta$ is the solar zenith angle (SZA). The radius of Mars is taken to be $R_{M}=3397 \mathrm{~km}$. Only the "northern" hemisphere is considered in this work.
here. Our main results are presented in $\S 3$ for several cases having different properties of the power spectrum of magnetic fluctuations, and a comparison with measurements is included. Finally, our conclusions are presented in § 4.

## 2. MODEL

We describe here the model used to study the motion of charged particles $\left(\mathrm{O}^{+}\right.$pickup ions) in a stationary background magnetic field with fluctuating magnetic and electric field components. The magnetic field configuration and the SW flow properties are taken to represent, as a first approximation, conditions present in the ionosheath of Mars. The geometry of our model is shown schematically in Figure 2, with several quantities identified below.

### 2.1. Equation of Motion

We follow the three-dimensional motion of particles in a time-dependent fluctuating magnetic field and its corresponding induced electric fluctuation. We will refer to such fluctuations as "turbulence", meaning that they have a particular power spectrum density distribution as discussed below. We treat only the non-relativistic motion of the pickup ions. We consider that the dynamics of these ions is determined solely by an electromagnetic interaction.

The equation of motion for a particle of mass $m$ and charge $q$, in a region with electric $\mathbf{E}$ and magnetic $\mathbf{B}$ fields is given, in the non-relativistic limit,
by the Lorentz equation (e.g. Jackson 1975):

$$
\begin{equation*}
\frac{d}{d t}(m \mathbf{v})=q\left(\mathbf{E}+\frac{\mathbf{v}}{c} \times \mathbf{B}\right) \tag{1}
\end{equation*}
$$

For the problem at hand, the magnetic field is assumed to be of the form:

$$
\begin{equation*}
\mathbf{B}(\mathbf{r}, t)=\mathbf{B}_{0}+\delta \mathbf{B}(\mathbf{r}, t) \tag{2}
\end{equation*}
$$

where $\mathbf{B}_{0}=\mathbf{B}_{0}(\mathbf{r})$ is the non-homogeneous stationary background field, while $\delta \mathbf{B}(\mathbf{r}, t)$ represents the turbulent part, with a zero-mean average value. No background electric field is considered here, so only that $\mathbf{E}$ resulting from the fluctuating $\delta \mathbf{B}$ will be taken into account in the equation of motion (see below).

### 2.2. Steady Background Fields

The steady fields determining the dynamics of the pickup ions are a non-homogeneous background magnetic field $\mathbf{B}_{0}$ and the streaming SW velocity $\mathrm{U}_{0}$; see Figure 2.

We are interested mainly in the dynamics of the ions over the terminator; hence our simulation region is restricted to a radial interval and $y$-coordinates given by, respectively:

$$
r \in\left[R_{p}, R_{\mathrm{out}}\right], \quad \text { and } \quad y \in\left[-\frac{R_{p}}{3},+\frac{R_{p}}{3}\right]
$$

where $r^{2}=x^{2}+z^{2}, R_{p}$ is the radius of the planet and $R_{\text {out }}$ is an external boundary; to be defined below. The regions $x>0$ and $z>0$ are the only ones considered for our numerical integrations.

The non-homogeneous background magnetic field used here resembles that present in non-magnetic planets. The magnetic field $\mathbf{B}_{0}$ in the $Y$-direction is taken to be essentially constant, but with a dependence on the coordinates $(x, z)$. For simplicity, we adopt the following analytical expression (RAP10) for this magnetic field, in component form:

$$
\mathbf{B}_{0}=\left[\begin{array}{c}
0  \tag{3}\\
\left(B_{\max }-B_{\min }\right) \cos \theta+B_{\min } \\
0
\end{array}\right]
$$

where $\cos \theta=x / r$, and $\left\{B_{\min }, B_{\max }\right\}$ correspond to values of the magnetic field at the polar $(\theta=\pi / 2)$ and sub-solar points $(\theta=0)$, respectively; see Figure 2 .

The velocity field $\mathbf{U}_{0}$ of the SW plasma around the planet is taken to increase sinusoidally in magnitude from the equator to the pole as:
$\mathbf{U}_{0}=\left[\begin{array}{c}-\left[\left(U_{\max }-U_{\min }\right) \sin \theta+U_{\min }\right] \sin \theta \\ 0 \\ +\left[\left(U_{\max }-U_{\min }\right) \sin \theta+U_{\min }\right] \cos \theta\end{array}\right]$,
where $\left\{U_{\min }, U_{\max }\right\}$ correspond to values at the subsolar points $(\theta=0)$ and polar $(\theta=\pi / 2)$ points, respectively, and $\sin \theta=z / r$.

### 2.3. Turbulent Magnetic Field

There is at the time being no general theory of turbulence in plasmas and there appears to be no unique way to describe it (e.g., Borovsky \& Funsten 2003; Cho, Lazarian, \& Vishniac 2003; Zhou, Matthaeus, \& Dmitruk 2004; Horbury, Forman, \& Oughton 2005; Galtier 2009). On the other hand, for example, the value of the spectral index of the SW turbulence being of a Kolmogorov or IroshnikovKraichnan type and its nature is still a matter of investigation (e.g., Bruno \& Carbone 2005; Ng et al. 2010).

In the case of homogeneous turbulence one may construct the magnetic field fluctuation $\delta \mathbf{B}$ at a particular spatial point by adding the contribution of a large set $\left(N_{m}\right)$ of plane waves with different wavenumber $(k)$. This can be done, for example, by means of a Fourier transform on $P(k)$ (e.g., Owens 1978) or by orienting randomly in space the wavevector number (e.g., Giacalone \& Jokippi 1994), with the field amplitude satisfying a particular form of the power spectrum.

Both the abbove approaches have their pros and cons (e.g., Casse, Lemoine, \& Pelletier 2002) and have been used in different works on the effects of turbulence. For example, in cosmic ray dynamics in the radio lobes of galaxies (e.g., Fraschetti \& Melia 2008; O'Sullivan, Reville, \& Taylor 2009) or for the acceleration of particles in shocks (e.g., Muranushi \& Inutsuka 2009). Here we consider the propagation of one-dimensional turbulent plane waves traveling in each perpendicular direction in turn, and assume homogeneous turbulence. This will allow us to assess the effect of maximum turbulence effects along each direction on the dynamics of the $\mathrm{O}^{+}$ions; which is the main objective of this work.

We write the magnetic fluctuation field at a particular point in space as a superposition of transverse plane waves propagating, for example, in the $\pm Z$-direction. Hence we write a $Z$-propagating wave with arbitrary polarization (e.g., Jackson 1975; Damask 2005) as the real part of:

$$
\delta \mathbf{B}=\left[\begin{array}{l}
\delta B_{x}  \tag{5}\\
\delta B_{y}
\end{array}\right]=\sum_{j}^{N_{m}} \delta b_{j}|p\rangle \mathrm{e}^{\mathrm{i}\left(k_{j} z-\omega_{j} t\right)}
$$

where the polarization state or Jones vector $|p\rangle$ in
the $X Y$-plane is given by

$$
|p\rangle \equiv\left[\begin{array}{c}
p_{x}  \tag{6}\\
p_{y}
\end{array}\right]=\left[\begin{array}{c}
\cos \varphi \mathrm{e}^{\mathrm{i} \phi_{x}} \\
\sin \varphi \mathrm{e}^{\mathrm{i} \phi_{y}}
\end{array}\right]
$$

with the $\varphi$ 's and $\phi$ 's being parameters describing the polarization state of the wave. For example, for $\phi_{x}=\phi_{y}$ we have a linearly polarized wave inclined at an angle $\varphi$, while if $\phi_{x}$ and $\phi_{y}$ differ by $\pi / 2$ circular polarization is produced; otherwise elliptical polarization is achieved.

The real value functions $\delta b_{j}=\delta b\left(k_{j}\right)$ in equation (5) are the fluctuating field amplitude corresponding to the $j$-th mode of the $m$-number of modes $N_{m}$. The frequency of oscillation of each mode is $\omega_{j}= \pm v_{\mathrm{ph}} k_{j}$, with $v_{\mathrm{ph}}$ being the phase-velocity of the $j$-th mode. For definiteness, the phase-velocity of the perturbations is taken here to be the Alfvén velocity of the plasma (i.e., $v_{\mathrm{ph}}=v_{A}$ ). The sign in the expression for $\omega_{j}$ accounts for waves traveling both in the positive or negative $Z$-direction, respectively. The form of turbulence represented in equation (5) satisfies, by construction, the divergence-free character of the magnetic field fluctuation $(\nabla \cdot \delta \mathbf{B}=0)$. A similar construction is done for each orthogonal propagation direction considered here.

The amplitudes $\delta b_{j}$ in equation (5) are chosen to satisfy a particular one-dimensional power spectrum of fluctuations $P(k)$. We assume here that the power spectrum density $P(k)$ is given by a power-law:

$$
\begin{equation*}
P(k)=P_{N}\left\langle\delta B^{2}\right\rangle k^{-\gamma} \tag{7}
\end{equation*}
$$

where $\left\langle\delta B^{2}\right\rangle$ is the magnetic field fluctuation variance, $\gamma$ the spectral index and $P_{N}$ a normalizing constant. For $\gamma=5 / 3$ we have a Kolmogorov (1941) turbulence and for $\gamma=3 / 2$ the Iroshnikov-Kraichnan type spectrum (Iroshnikov 1963; Kraichnan 1965). The normalization of the spectrum is such that

$$
\begin{equation*}
\int_{0}^{\infty} P(k) \mathrm{d} k=\left\langle\delta B^{2}\right\rangle \tag{8}
\end{equation*}
$$

In practice, the limits of integration in equation (8) go from $k_{\min }$ to a $k_{\max }$, dictated essentially by numerical criteria of the calculations.

The discrete amplitudes $\delta b_{j}$ in equation (5) can now be obtained from the power spectrum (equation 7 ). Using the orthogonality of the polarization state vector,

$$
\langle p \mid p\rangle \equiv\left[p_{x}^{*}, p_{y}^{*}\right]\left[\begin{array}{c}
p_{x} \\
p_{y}
\end{array}\right]=1
$$

where $\langle p|$ is the complex conjugate (dual) vector of $|p\rangle$, and $\left\langle\delta B^{2}\right\rangle=\delta \mathbf{B} \cdot \delta \mathbf{B}^{\dagger}$, and assuming statistical


Fig. 3. Intensity plot of a particular turbulent magnetic field realization of plane waves traveling in the $Z$-direction at different times. The $X$-component is shown in the left figure while the $Y$-component in the right one. The total field variance here is $\left\langle\delta B^{2}\right\rangle=1$ and $\gamma=2$. Units are arbitrary. The color figure can be viewed online.
independence among the different wave modes, we have

$$
\begin{equation*}
\sum_{j=1}^{N_{m}} P\left(k_{j}\right) \Delta k_{j}=\sum_{j=1}^{N_{m}} \delta b_{j}^{2} \rightarrow \delta b_{j}^{2}=P\left(k_{j}\right) \Delta k_{j} \tag{9}
\end{equation*}
$$

The numerical realization of our turbulent magnetic field is obtained as follows. Given a mean fluctuation $\left\langle\delta B^{2}\right\rangle$, a spectral index $\gamma$ and $\left\{k_{\min }, k_{\max }\right\}$ for the fluctuations, a normalization constant $P_{N}$ is determined from equation (8). We choose a set of $N_{m}$ equally spaced wave-numbers in $\log k$-space in the relevant interval. From this set of $k$ values, the amplitudes $\delta b_{j}$ are obtained using equation (9). Since we are not interested in any particular effect of the polarization state of the turbulent waves, we choose random phase values $\phi_{x}$ and $\phi_{z}$ and angle $\varphi$ in equation (6) uniformly distributed in $[0,2 \pi]$ for each $k_{j}$ value.

At each point, for example $z$, and time $t$, the sum in equation (5) is evaluated, and the $\delta B_{x}$ and $\delta B_{z}$ components are obtained. In this form, the total magnetic fluctuation $\delta \mathbf{B}$ is constructed; which is to be added to the inhomogeneous background field $\mathbf{B}_{0}$ of equation (2). A similar construction is done for each propagation direction of turbulent waves when required. In Figure 3 we show a particular random realization of a turbulent field.

### 2.4. Electric Field

In the stationary reference frame the electric field depends on the local total velocity field of the SW plasma $\mathbf{U}$ around the planet and the local magnetic field. In the non-relativistic limit this leads to

$$
\begin{equation*}
\mathbf{E}(\mathbf{r}, t)=-\frac{1}{c} \mathbf{U} \times \mathbf{B}(\mathbf{r}, t) \tag{10}
\end{equation*}
$$

where $\mathbf{B}$ is the total magnetic field obtained from equations (5) and (3). The total velocity field $\mathbf{U}$ is obtained as $\mathbf{U}=\mathbf{U}_{0}+\delta \mathbf{U}$, where we consider that $\delta \mathbf{U}(\mathbf{r}, t)=-v_{A} \delta \mathbf{B} / B_{0}$ as in a MHD Alfvénic wave.

The fields determined by equations (2) and (10) are used in equation (1) to determine the dynamics of each pickup $\mathrm{O}^{+}$ion in the ionosheath of Mars.

### 2.5. Initial Conditions and Integrator

For a particular mode in the plane-wave expansion (equation 5) one expects that if the time-scale $(\sim 1 / \omega)$ for the field fluctuation is about the same as the time-scale of gyrotropic motion of the ions $(\sim 1 / \Omega$, with $\Omega=q B / m c)$, the dynamics of the particles will be drastically affected. On other hand, in order for an Alfvénic-type turbulence to affect the motion of pickup ions it has to modify such motion in the time scale necessary for the ion to transverse our region of interest; e.g., from the subsolar point to the terminator. These considerations guide us, as well as in situ measurements, to adopt some numerical values for different parameters in our calculations.

The turbulence spectrum index is taken to be $\gamma=2$ in concordance with measurements in the ionosheath of Mars. The amplitude of the turbulent component of the magnetic field is parameterized by the energy ratio $\varepsilon=\left\langle\delta B^{2}\right\rangle / B_{0}^{2}$, and we have considered the particular values $\varepsilon=(0.0,0.1,0.5,1.0)$.

The equation of motion (equation 1) for each ion was solved using a fourth order Runge-Kutta algorithm with an adaptive time-step instead of the standard Buneman-Boris algorithm (e.g., Birdsall \& Langdon 1985), a time-symmetric second-order scheme, used in plasma dynamics. This was adopted after several numerical tests with both integrators,


Fig. 4. Trajectories of $\mathrm{O}^{+}$ions in a model of the ionosheath of Mars on the $X Z$-plane. Only a turbulence power of $\varepsilon=0$ and 1 has been considered here. The direction of the turbulent wave propagation vector $k$ is indicated in each panel. The color figure can be viewed online.
and by the requirement of following more accurately the trajectories of particles especially when a large amplitude of turbulence $(\varepsilon \approx 1)$ and rapid oscillations were present in the Martian ionosheath.

A total of $10^{5}$ charged particles was used for each value of $\varepsilon$ and propagation direction of turbulent waves considered, yielding a total of one million particle integrations in our numerical experiments. The $10^{5}$ particles were obtained from sets of $10^{4}$ particles evolved in 10 different random realizations of the power spectrum $P(k)$, using each time a different initial seed for the random number generator required to construct the turbulent $\delta \mathbf{B}$. Particles were distributed spatially only in the "upper" dayside of Mars, and following an exponential density decay with altitude as in RAP10.

As our fiducial model for the ionosheath of Mars we adopt the following set of values for different pa-
rameters in our model. The range in magnetic field is taken as $\left(B_{\min }, B_{\max }\right)=(4,7) B_{0}$, where $B_{0}=5 \mathrm{nT}$, that we choose based on the data from Bertucci et al. (2003). The SW plasma velocity is taken as $V_{\mathrm{SW}}=400 \mathrm{~km} \mathrm{~s}^{-1}$ and the Alfvén velocity of waves $v_{A}=0.1 V_{\mathrm{SW}}$. The range of velocities of the SW plasma flow around the planet is assumed to be $\left(U_{\min }, U_{\max }\right)=(0.01,0.5) V_{\mathrm{SW}}$, consistent with values measured in that region; see for example the data in Figure 1. Under these conditions, the mean local cyclotron frequency for a proton in our region of interest is $f_{p}=\Omega_{p} / 2 \pi=0.42 \mathrm{~Hz}$; where the mean field is taken to be $\langle B\rangle=5.5 B_{0}$. The range of frequencies for the turbulence spectrum is taken from $f_{\text {min }}=f_{p} / 16 \approx 0.03 \mathrm{~Hz}$ to $f_{\max }=30 f_{p} \approx 13 \mathrm{~Hz}$, which is consistent with the range in $P(k)$ measured in the ionosheath of Mars (e.g., see Figure 5b in Grebowsky et al. 2004). For the $v_{A}$ chosen, the follow-


Fig. 5. As in Figure 4 but for motion projected on the $Y Z$-plane. The color figure can be viewed online.
ing range in length-scales $(\lambda=2 \pi / k)$ is obtained $\left(\lambda_{\min }, \lambda_{\max }\right) \approx(3.2,1526) \mathrm{km}$.

## 3. RESULTS

In this section we present results obtained for the motion of $\mathrm{O}^{+}$ions under different conditions of turbulence. We first present the space trajectories of the ions and afterwards their velocity profiles at the terminator.

### 3.1. Ion Trajectories

In Figure 4 we show twenty random trajectories of $\mathrm{O}^{+}$ions in the $X Z$-plane for turbulent waves propagating in the $x, y$ and $z$-direction for the extreme amplitude $\varepsilon=1$, along with the $\varepsilon=0$ case, and in Figure 5 the corresponding ones in the $Y Z$-plane. The rectangular box in these figures corresponds approximately to an altitude range from 300 km to 2300 km; see Figure 1.

The motion of pickup oxygen ions without turbulence $(\varepsilon=0.0)$, is qualitatively similar to that found in previous works on the dynamics of pickup ions with an analytical model for the B-field (e.g., Luhmann \& Schwingenschuh 1990; Luhmann 1990; Kallio \& Koskinen 1999; RAP10) and to that derived from MHD simulations (e.g., Jin et al. 2001; Bößwetter et al. 2007; Fang et al. 2008; Fang et al. 2010).

The presence of even a small amplitude $(\varepsilon=0.1)$ of turbulent waves propagating in the ionosheath has a strong effect in the $Y Z$-motion of pickup ions, while it is less noticeable in the $X Z$-plane. Even in the case of $\varepsilon=1.0$ the $X Z$-motion is not greatly affected (Figure 4); in particular, the trajectories are not importantly "bent" toward the SW direction of motion as inferred from the Mars-Express measurements (Figure 1).

The dynamics of pickup ions is clearly very complex even under a small "perturbation" to the back-


Fig. 6. Phase-space diagrams of $\mathrm{O}^{+}$ions at the Martian terminator: $V_{z}-z$ and $\left|V_{x}\right|-z$. Turbulent waves propagating in the $X$-direction of increasing amplitudes $\varepsilon$ are shown from left to right.
ground field that, for example, may preclude any estimation of the ionosheath conditions based solely on the analysis of the motion of pickup ions. The analysis of the statistical motion of the ions is beyond the scope of this paper, but we expect that they will have dynamics similar to that of Lévy random walk process (e.g., Shlesinger, West, \& Klafter 1987; Greco et al. 2003).

### 3.2. Velocity Profiles

Several processes may be investigated from the velocities of the ions in the turbulent medium, such as their phase-space structure or the pitch-angle difussion and scattering (e.g., Price \& Wu 1987; Li et al. 1997; Cravens et al. 2002; Fang et al. 2008). Although important for our understanding of $\mathrm{O}^{+}$ pickup ions, our focus here is essentially on the vertical velocity profiles of the ions over the terminator in order to compare them with the data shown in Figure 1.

The vertical velocity profiles of $\mathrm{O}^{+}$ions were computed at the terminator, and considering only a small region of width in the $Y$-direction of $\Delta y=$ $\pm R_{M} / 4$; as indicated in Figure 5. Twenty bins in the $Z$-direction were set and the average velocity of all particles crossing the terminator was computed for each component. This was done for each level of turbulence and each direction of the Alfvénic waves.

In Figure 6 we show "phase-space" plots of the particles above the Martian terminator, in the box described above, for our fiducial parameters. The different graphs correspond to different levels of turbulence $(\varepsilon=0,0.1,1)$ propagating in the $X$ direction. A clear effect of heating and scattering in phase-space due to turbulence is appreciated as its
amplitude $\varepsilon$ increases in value. Under our fiducial values, and with the different prescriptions for turbulent waves, we notice already from Figure 6 that the $Z$-component of the velocity dominates over the $X$-component.

In Figure 7 we show the average velocities of $v_{x}$, $v_{y}$ and $v_{z}$ of the $\mathrm{O}^{+}$ions, for turbulence amplitudes $\varepsilon=0.1$ (top) and $\varepsilon=1.0$ (bottom). The case of $\varepsilon=0$ has a behavior similar to that of $\varepsilon=0$ and we do not consider it in Figure 7. The graphical representation is similar to that in Figure 1 in order to aid in the comparison with the in situ data; the $Z$ component of the velocity has been inverted in sign for that purpose.

The trend displayed by the velocity profiles is similar to that reported in RAP10, although significant differences appear now when turbulent waves are taken into account. In the non-turbulent case, $\varepsilon=0$, the $\left\langle v_{y}\right\rangle$ is zero since no motion along the $Y$-direction is generated (see Figure 5). Once a turbulent component sets in, the erratic motion of particles contributes to a non-zero value of $\left\langle v_{y}\right\rangle$.

A clear result from all of our numerical calculations is that even under a strong $(\varepsilon=1)$ level of turbulent waves propagating in any direction, the trend of the $Z$-component of the velocity of ions always dominating over the $X$-component is preserved, contrary to measurements at such altitudes in the Martian terminator.

Unfortunately, for example, the extensive and complete MHD simulations of Fang et al. (2008) do not address the velocity profiles of pickup ions at the terminator, so we are not able to compare our results with their work. In this respect, it will be interesting to measure from this kind of MHD simu-


Fig. 7. Vertical velocity profiles of $\mathrm{O}^{+}$ions at the Martian terminator. From left to right, the plots correspond to different turbulent wave propagation vector. The upper row corresponds to values of $\varepsilon=0.1$ and the lower to $\varepsilon=1.0$.
lations the vertical profiles of $\mathrm{O}^{+}$ions and compare them with data.

## 4. DISCUSSION AND FINAL COMMENTS

### 4.1. Discussion

We have calculated the trajectory and average velocity profiles of newly born $\mathrm{O}^{+}$ions in the dayside ionosheath and magnetic polar regions of Mars, as they are accelerated by the convective electric field due to the streaming solar wind plasma. In addition to a simplified model of the draped IMF, which determines the large-scale geometry of the magnetic field, we have included for the first time an approximation to the "turbulent" component for the magnetic field in that region, and studied its effect on the dynamics of pickup ions. We have compared the velocity profiles resulting from our calculations to those measured in the region with the ASPERA-3 instrument onboard the Mars Express, as reported by PdT09.

The effect of a turbulent part $\delta \mathbf{B}$ on the magnetic field is most significant in deflecting the trajectories
in the plane perpendicular to the SW flow (plane $Y Z$ ), but it has little effect on modifying the velocity structure of pickup ions at the terminator in comparison to the absence of turbulent waves. This behavior holds under different power-laws $(\gamma)$ for the turbulence power spectrum and its amplitude $(\varepsilon)$, as well as for its direction of propagation and small variations of our fiducial values ( $\S 2.5$ ) of the parameters in the simulations.

In searching for a pure dynamical explanation of the velocity profiles measured by the Mars-Express spacecraft, we decided to use parameters in our model that would probably favor the dominance of the $V_{x}$ component over the $V_{z}$ component. For this, we would require a strong magnetic field at the poles, $B_{\min }$, and a small velocity $U_{\max }$, since the gyro-radius of a particle, for the same $q / m$ ratio, is $r_{g} \propto v_{\perp} / B$ and this would make the trajectories bend more, and at the terminator the $X$-velocity would be increased.

We decided to use for a new set of runs with $B_{\min }=6 B_{0}=30 \mathrm{nT}$ and $U_{\max }=0.375 V_{\mathrm{SW}}=$


Fig. 8. The same as in Figure 6 but with parameters more favorable for a strong curvature in the paths of $\mathrm{O}^{+}$ions. An increase of particle density in different regions of the phase-space is noted in comparison to that of Figure 6.
$150 \mathrm{~km} \mathrm{~s}^{-1}$, and kept the rest of the parameters the same as in our fiducial case. As one might expect there is a dominance of the $V_{x}$ component over the $V_{z}$, but this occurs only for certain altitudes as shown in Figures 8 and 9. Even with these values of the parameters, rather extreme according to the data (see, for example, Figure 1 from which an estimate of $U_{\text {max }}$ can be obtained) the behavior of the profiles does not correspond to the measurements; for example, no inversion of the velocity profiles at altitudes $\approx 1000 \mathrm{~km}$ is present. This numerical experiment strongly suggests that even under favorable conditions (albeit not consistent with measurements of the properties of the $B$-field and stream velocity of the SW at the pole) the idea of the behavior of $\mathrm{O}^{+}$being due to charge-particle dynamics is not sustainable.

On the basis of our results, we conclude that turbulent-like magnetic field fluctuations, and the accompanying convective electric field variations, are not likely to influence the dynamics of picked-up $\mathrm{O}^{+}$ ions in a manner sufficient to explain their essentially tailward velocity measured over the magnetic pole of Mars. Furthermore, the relative behavior of the different components of the velocity obtained in particle simulations does not correspond to what is measured at the Martian terminator. This suggests that processes additional to a purely charged-particle dynamics must be playing a dominant role in the interaction of the collisionless solar wind and the ionospheric plasma in the region.

A possibility is advocated by Pérez-de-Tejada and collaborators (e.g., Pérez-de-Tejada \& Dryer 1976; Pérez-de-Tejada 1999; PdT09; RPAV10), where a viscous-like interaction of the SW plasma
and the ionosheath plasma is occurring. The interaction of the SW with the upper ionosphere over the magnetic polar regions of non-magnetic planets and objects is characterized by the existence of several features that lend themselves to be explained in terms of fluid viscous-like interaction. Several of the phenomena for which this provides an explanation are briefly summarized here for the sake of completeness. (1) The existence of a velocity shear in the ionosheath as spacecraft approach Venus over the magnetic poles (Romanov, Smirnov, \& Vaisberg 1979; Bridge et al. 1967; PdT09). The accompanying decrease in the plasma density and the increase in the gas temperature are consistent with a viscouslike boundary layer in the region. (2) A similar situation is observed in the ionosheath of comet Halley below the so-called "mystery transition", where the decrease in SW velocity and density and the simultaneous increase in the gas temperature, measured by the Giotto spacecraft, is consistent with a viscouslike flow characterized by an effective Reynolds number $\approx 30$ (Pérez-de-Tejada 1989; RPAV10). (3) The transterminator flow observed by the Pioneer Venus Orbiter ( $P V O$ ) is consistent with a viscous-like dragging of the Venus upper ionosphere by the SW flow (Pérez-de-Tejada 1989). Since such interaction occurs preferentially over the magnetic polar regions this leads to the carving-out of plasma channels in the ionosphere and near wake, providing a simple explanation for the ionospheric holes measured by PVO in the nightside of the planet (Pérez-de-Tejada 2001, 2004). It is important to indicate that the physical nature of such "anomalous viscosity" is not addressed in these papers, and will be the subject of future investigations.


Fig. 9. As in Figure 7 but with a stronger $B_{\min }=30 \mathrm{nT}$ and lower $U_{\max }=150 \mathrm{~km} \mathrm{~s}^{-1}$ in order to favor an increase in the curvature of the $\mathrm{O}^{+}$pickup ions and its $V_{x}$ component. Note that the general behavior of the profiles does not correspond to the ASPERA-3 measurements.

### 4.2. Final Remarks

It must be stressed that the calculations presented in this paper are not fully self-consistent, in the sense that the electromagnetic field and the solar wind velocity around the Martian ionosheath are assumed, not solved for. Nonetheless, the assumed SW velocity field and $B$-field structure are representative of what might be the Martian magnetic field in the region of interest; the case of the southern hemisphere would be more complex to model due to the presence of inhomogenieties due to crustal fields.

The type of approach taken here clearly prevents us from studying plasma instabilities which may play an important role in the coupling of solar wind and ionospheric plasma and significantly change our conclusions. The effect of such instabilities on the dynamics of $\mathrm{O}^{+}$ions, as well as that of magnetic field features related to its 3D character and the presence of magnetic concentration regions, are beyond the scope of the present study and will be treated in future contributions.

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