Cultivation shifts in forest plantations of *Eucalyptus grandis* Hill ex Maiden, in *Uruapan, Tabasco*

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Abstract:

Commercial timber plantations in Mexico have become an opportunity for increasing the production and productivity of the subsector, as well as for reducing the pressure on the natural forest areas and increasing the income of rural families. The objective of this research was to analyze the relationship and behavior between three different types of shifts: 1) Technical: Maximum Average Production (MAP) and Maximum Total Production (MTP); 2) Economic: Hotelling and Faustmann; and 3) economic-environmental: Hartman—in plantations of *Eucalyptus grandis* in the municipality of *Balancán, Tabasco*, Mexico, and to provide elements that may contribute to decision-making in the forestry companies. Data from three inventories provided by the company *Productora de Plantaciones del Sureste* were used. The type of average interest rates of the certificates of the Treasury of the Federation (CETES) (8 %), an average price of $107.00 tCO₂e⁻¹ (tab average used by the European Climate Exchange Carbon from 2010 to 2014), a cost of establishment of the planting of $38 000 ha⁻¹, a price of roundwood of $650.00 m⁻³, and a cost of $2 000.00 ha⁻¹ yr⁻¹ were considered. The estimated shifts were the following: MAP (10.24 years), Faustmann (10.82 years), Hotelling (11.32 years), Hartman (11.64 years) and MTP (97.2 years). We conclude that the number of years increases as economic-environmental aspects are incorporated in the estimation of shifts.

Keywords: Carbon capture; forestry companies; Schumacher growth model; economic shifts; environmental-economic shifts; technical shifts.
Introduction

With the incorporation of Mexico to the General Agreement on Tariffs and Trade (GATT) in 1986 and the entry into force of the North American Free Trade Agreement (NAFTA) in 1994, the pressures on the country’s natural resources increased. Authors such as Barton and Merino (2004) speculate that these have been factors that contribute to the deterioration of forest resources. However, they are not exclusive of free trade; there are causes that go beyond commercial exchanges —e.g. poor forest management plans, the growing urban sprawl, the increase in agricultural land and pastures for livestock, and illegal logging.

Historically, the timber production in Mexico comes from natural forests (Álvarez et al., 2015; Luján et al., 2016); on average, during the period of 1990 to 2014, 84 % of the production came from coniferous forests, 11 percent, from broadleaf forests, and 5 %, from tropical forests (Semarnat, 2014). This is why special attention was given to the estimation of biological or technical shifts (Semarnat, 2010).

In 1995, the establishment of commercial timber plantations (CTPs) was encouraged with the three-fold purpose of increasing the production and productivity of the raw materials subsector, reducing the pressure on the natural forest areas, and increasing the income of rural households (Luján et al., 2016). Moreover, they emerged as a productive option to convert agricultural land that had lost its vegetation into forest land capable of producing raw materials to supply the forest industry and provide ecosystem services (Conafor, 2016). Andreoni and Bussoni (2014) point out that the growing demand for timber products can be addressed by means of an adaptive strategy through genetic improvement in plantations.
On the other hand, with the implementation by CONAFOR of the National Strategy of Sustainable Forest Management to increase the production and productivity (Enaipros) 2013-2018 and of the National Strategy for REDD+ (Reducing Emissions from Deforestation and Forest Degradation), one of the greatest challenges is to increase the forest timber production and to reduce the emission of greenhouse gases; therefore, CTPs are considered to be a viable option for the achievement of these objectives (Geréz and Pineda, 2011; Conafor, 2016).

The implementation of both strategies has promoted the establishment of CTPs of fast-growing tropical species such as *Tectona grandis* L. F., *Gmelina arborea* Roxb., *Cedrela odorata* L., and *Eucalyptus grandis* Hill ex Maiden (Conafor, 2016). This brought about the need for viable forest shifts according to the current necessities (technical, economic shifts and economic-environmental).

The application of the theory of the economically optimal shift in CTPs has not been addressed with sufficient profusion by the forestry literature of Mexico. Authors such as Medema and Lyon (1985), who wrote one of the first papers that dealt with the issue, applied Faustmann’s formulation and solution, proposed in 1849, using an iterative procedure for the calculation of the optimal age. Tait (1986), Chang (1998), and Smart and Burgess (2000) utilized the formulation with a generalized solution, using dynamic programming. As for the forest shifts, which incorporate as input the timber production and carbon capture, they have been cited since the 1990s (Hoen and Solberg, 1994; Van *et al.*, 1995; Romero *et al.*, 1998).

Although, studies of forest shifts have been carried out at the international level, the basic issues of forest management and exploitation in Mexico revolve around the few efforts made to research appropriate shifts and, to a greater extent, for the State of Tabasco, despite its being one of the main entities with CTPs (Conafor, 2016).
This research posed the following hypothesis: as environmental aspects are incorporated in the estimation of the economic shifts, the optimal felling age is greater, resulting in a lengthening in the number of years of the forest shift. The objective was to analyze the behavior and the relationship between three types of forest shifts in commercial plantations of *Eucalyptus grandis* Hill ex Maiden located in Balancán, Tabasco, Mexico, by calculating three shifts—technical, economic and environmental-economic—, as well as to provide elements that may contribute to decision-making in the forestry companies.

**Materials and Methods**

**Study area**

The study area is located in the municipality of Balancán in the *Usumacinta* region of Tabasco, Mexico. It is located at the coordinates 17°48' N and 91°32' W. It borders Campeche to the north, the municipalities Tenosique and Emiliano Zapata to the south, the state of Campeche and the Republic of Guatemala to the east, and the municipality of Emiliano Zapata and Campeche to the west (Municipios.mx, 2016) (Figure 1).
Figure 1. Location of the study area.

Adjusted growth model

A Schumacher growth model relating the volume of wood to age and assuming that the rate of growth varies inversely with age, was adjusted (López and Valles, 2009).

\[
V(t) = \beta_0 \exp \left[ -\beta_1 \left( \frac{1}{t} \right) \right]
\]

\((1)\)
Where:

\[ V(t) = \text{Volume of timber in the year } t \ (m^3\text{tree}^{-1}) \]

\[ t = \text{Age (years)} \]

\[ \beta_i = \text{Parameters, to } i = 0 \text{ and } 1 \]

**Forest shifts**

Five forest shifts were estimated: two technical shifts (maximum total production and maximum average production), two economic shifts (Hotelling 1931, and Faustmann 1849) and one economic-environmental shift (Hartman, 1975). The last three were based on the determination of the monetary value of the timber production, as suggested by Romero et al. (1998).

Technical shifts. The technical approach involves a bare analysis, due to its low complexity for manipulating the growth or the production function. The maximum total production occurs at the highest point of the production function; thus, the optimal felling shift is when the marginal production is equal to zero. Likewise, the maximum average production is obtained by dividing the production function by the age of the plantation \((t)\) (Bonilla and Alarcón, 2015).

Economic Shifts. In forest economy and management this is a concept that incorporates economic aspects such as production costs, timber prices and interest rate. Given their theoretical and practical importance, two economic shifts were analyzed: Hotelling’s formulation of 1931, and Faustmann’s approximation of 1849 (Díaz, 1997).

The procedure suggested by Hotelling consists in maximizing the Current Net Value (CNV) of the investment:
MaxCNV = pV(t)exp(−it) − k .................................(2)

Where:

\( p \) = Price of timber (MXN)

\( V(t) \) = Volume of timber in the year \( t \) (m\(^3\) tree\(^{-1}\))

\( i \) = Type of discount

\( t \) = Age (years)

\( k \) = Cost of the plantation (MXN tree\(^{-1}\))

Therefore, the condition of balance of Eq. 2 is given by the following expression.

\[
\frac{V'(t)}{V(t)} = i .................................(3)
\]

Where:

\( V'(t) \) = Marginal timber product in the year \( t \)

The model suggested by Faustmann includes a land rent variable; thus, the expression Eq. 2 becomes:

\[
MaxCNV = pV(t)exp(−it) − k − \int_{0}^{t}exp(−it)dt  .........................(4)
\]
Where:

\[ R = \text{Land rent (MXN)} \]
\[ dt = \text{Age differential} \]

and the condition of balance of Eq. 4 is:

\[
\frac{V'(t)}{V(t)} - \frac{R}{pV(t)} = i \quad \text{(5)}
\]

Environmental-economic shift. The basic idea of Hartman is to introduce a function \( G(t) \) that measures the flow of non-timber (environmental, recreational, or ecosystem) services or income generated by a forest mass with an age of \( t \) years, in addition to the production curve \( V(t) \) (Romero, 2001). The Hartman model posed is:

\[
\text{MaxVAN} = pf(t) \exp(-it) + G(t) - R \int_0^t \exp(-it) dt - k \quad \text{(6)}
\]

Where the condition of balance is given by:

\[
\frac{V'(t)}{V(t)} - \left[ \frac{R - G(t)}{pV(t)} \right] = i \quad \text{(7)}
\]
The non-timber yield curve suggested by Hartman is a production function in which the marginal productivities may decrease but are never negative. The function $G(t)$ is calculated based on the value of the carbon captured in the plantation.

**Estimation of carbon capture**

The accumulated (captured) carbon per hectare was estimated in terms of the volumetric yield, based on the amount of carbon per m$^3$ of wood. The density of the wood and the carbon content of biomass estimated with the procedure of Smith et al., (1993) were considered.

The amount of CO$_2$e (carbon equivalent) of Table 1 includes only the carbon contained in the biomass of the stem; that of the branches and foliage was calculated using conversion factors of total aerial biomass, based on the biomass of the stem. The production of biomass of the stem in relation to the total area for *Eucalyptus grandis* Hill ex Maiden was 88 %; therefore, the conversion factor was: $100/88=1.136$. Thus, the total amount of CO$_2$e per m$^3$ of timber was 0.919 tonnes.

<table>
<thead>
<tr>
<th>Variable</th>
<th>\textit{Eucalyptus grandis}</th>
</tr>
</thead>
<tbody>
<tr>
<td>Density (t m$^{-3}$)</td>
<td>0.46</td>
</tr>
<tr>
<td>Content of carbon in biomass (percentage in decimal form)</td>
<td>0.48</td>
</tr>
<tr>
<td>Carbon/volume ratio (tC m$^{-3}$)</td>
<td>$0.46 \times 0.48 = 0.22$</td>
</tr>
<tr>
<td>CO2e/timber volume ratio (tCO$_2$e m$^{-3}$)$^+$</td>
<td>$0.22\left(\frac{44}{12}\right)^{++} = 0.809$</td>
</tr>
</tbody>
</table>

\*Table 1. Estimation of carbon capture by *Eucalyptus grandis* Hill ex Maiden.*
The value of the benefits obtained from carbon capture $G(t)$ was estimated using the approach of Van et al. (1995) as modified by Stainback and Alavalapati (2002):

$$G(t) = p_c \cdot \alpha \left( V(t) \cdot \exp(-it) + \int_0^t V(t) \cdot \exp(-it) dt \right) - \frac{p_c \cdot \alpha \cdot \beta \cdot V(t) \cdot \exp(-it)}{\pi_{CO_2\text{des}}}$$

Where:

$G(t)$ = Net value of the benefits from carbon capture (MXN)

$\pi_{CO_2\text{Tot}}$ = Total value of the standing tree due to carbon capture (MXN)

$\pi_{CO_2\text{Des}}$ = Value discounted due to the harvested timber products (MXN)

$p_c$ = Price of carbon (S/tCO$_2$e)

$\alpha$ = Constant expressing the proportion of CO$_2$e per m$^3$ of timber

$V(t)$ = Volume of timber in the year $t$ (m$^3$ tree$^{-1}$)

$i$ = Type of discount

$t$ = Age (years)

$dt$ = Age differential

$\beta$ = Discounted proportion of the harvested timber

A value equal to $\beta$ 0.10 was considered; i.e. 10 % of the captured carbon is released in the whole process of harvesting and sawmilling.
**Provenance of the information**

Data from three national forest inventories (2009, 2010 and 2011) carried out by the company "Productora de Plantaciones del Sureste" (Proplanse) in plantations of *Eucalyptus grandis* in the municipality of Balancán, Tabasco, Mexico, were used in the present research. A random stratified sampling design was utilized, and sites of fixed dimensions were defined as sampling units. The equation for cubing standing trees, which is a modification to the Australian model, was obtained from Proplanse.

\[
V = 0.00003805 - 0.00009789 * d^2 + 0.0001325 * d * a + 0.00002967 * d^2 * a
\]

Where:

- \( V \) = Volume in cubic meters without the bark (m\(^3\))
- \( d \) = Normal diameter in meters (m)
- \( a \) = Total tree height in meters (m)

The average interest rate or discount provided by the certificates of the Treasury of the Federation (CETES) (8 %) and an average price of carbon of $107.00 per tonne of CO\(_2\)e (average tabulator utilized by European Climate Exchange Carbon from 2010 to 2014) were considered. The data related to the cost of the plantation ($38 000 ha\(^{-1}\), MXN), the price of wood ($650 m\(^{-3}\), MXN) and the rent of land ($2 000 ha\(^{-1}\) year\(^{-1}\), MXN) were provided by the company Proplanse.


Results and Discussion

The Schumacher production function was formulated based on the results of this study.

\[ V(t) = 1.040509 \cdot \exp\left(-10.249764\left(\frac{1}{t}\right)\right) \quad \forall t \geq 0 \quad \ldots \ldots \ldots (9) \]

The production function shows a high correlation coefficient \( R^2 = 0.9989 \), which is indicative of an adjustment, as well as low levels of Sum of Squares of the Error \( SCE = 0.00062 \).

Technical shifts. The Schumacher-type function has a horizontal asymptote, which implies that it does not decrease. To this end, we obtained an approximation by discriminating 10 % of the total production, since the marginal increases are minimal, as shown:

\[ (1-\alpha)\lim_{t \to \infty} V(t) \]

Where:

\( \alpha = \) Percentage of production for discrimination (10 % in this study)

By solving this equation and replacing in the production function (Eq. 9), the Maximum Total Production (MTP) is shown to be attained at 97.20 years of
age of the plantation. The Schumacher production function turned out to be an inappropriate model for the calculation of the MTP, whereas the adjusted model allows projecting it 25% into the future, according to Montgomery et al. (2007); i.e. it predicts acceptably up to the 19th year (the information presented is indicative).

The Maximum Average Production (MAP) corresponds to 10.24 years of age of the plantation (Figure 2).

\[ Volumen = \text{Volume}; \quad Edad = \text{Age} \]

**Figure 2.** Marginal Production Curves (PMg) and Mean Product (PMe) for *Eucalyptus grandis* Hill ex Maiden, derived from the adjusted Schumacher function.

Economic shifts. Once the economic values in the formulations of Hotelling and Faustmann had been replaced, the balance curves were calculated for each formulation, being of 11.32 years for Hotelling’s shift, and 10.82 years for Faustmann’s (Figure 3, Table 2).
$VAN = CNV$ (Current Net Value); $Edad$ = Age

**Figure 3.** Hotelling, Faustmann and Hartman equilibrium curves for *Eucalyptus grandis* Hill ex Maiden, derived from the adjusted Schumacher function.

**Table 2.** Overview of the forest shifts estimated for *Eucalyptus grandis* Hill ex Maiden.

<table>
<thead>
<tr>
<th>Shifts</th>
<th>Type</th>
<th>Forest shift (years)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Technical</td>
<td>Maximum total production</td>
<td>97.20</td>
</tr>
<tr>
<td></td>
<td>Maximum average production</td>
<td>10.24</td>
</tr>
<tr>
<td>Economic</td>
<td>Hotelling</td>
<td>11.32</td>
</tr>
<tr>
<td></td>
<td>Faustmann</td>
<td>10.82</td>
</tr>
<tr>
<td>Economic-Environmental</td>
<td>Hartman</td>
<td>11.64</td>
</tr>
</tbody>
</table>
Environmental-economic shift. The balance function, whose shift is reached at 11.64 years of age, was calculated by integrating the economic and environmental values (Figure 3, Table 2).

The estimated forest shifts constitute a novel contribution to investors both in the CTPs of the municipality of Balancán, Tabasco, and in certain places with similar biophysical characteristics to those of the study area, since they may be used as a reference point in the forest management of the plantations.

According to Frangi et al. (2016) and Santiago et al. (2015), *Eucalyptus grandis* has a rapid growth; for this reason, the forest shifts are short compared to those of other species destined for sawmilling. The following is a brief comparison and a description of the relationship between the five shifts considered.

A growing relationship was observed in the shift rotation with the incorporation of environmental and economic variables such as the carbon capture. In general terms, the rotation has diminished as a larger number of economic aspects (costs) are considered in its determination; conversely, it has increased with the inclusion of environmental and recreational aspects (income). The corresponding behavior was as follows: Maximum Average Production (10.24 years), Faustmann shift (10.82 years), Hotelling shift (11.32 years), Hartman shift (11.64) and Maximum Total Production (97.20 years).

In the analysis of shifts, the Hartman shift was observed to increase by 3.2 months compared to the Hotelling shift; in relation to the Faustmann shift, the increase was 9.8 months, and with regard to the MAP, it was 16.8 months.

Similar data were estimated in the state of Oaxaca for this species (Téllez et al., 2008), after analyzing two scenarios —1) wood for cellulose and 2) wood for sawmilling and pulp— with an economic approach. In the first scenario, the shift
was determined to range between 6.9 and 9.0 years, while for the second, it ranges between 9.0 and 13.5 years; when an income for carbon capture was incorporated into the calculation, the shift increased between 12 and 20, and 17 and 30 months, respectively. Certain authors consider that the forest shifts of *Eucalyptus grandis* in Colombia range between 6 and 8 years (Restrepo and Alviar, 2010; Gómez *et al.*, 2012).

It is worth mentioning that the extension of the forest shift is a consequence of the genesis (structure) of each model, and that it favors the generation of (larger quantities of) heartwood and the capture of carbon. Dias *et al.* (2016) points out that for the genus *Eucalyptus* short shifts result in good growth rates but a poor quality as wood, as pulp for the manufacture of paper, and for the drying process. Therefore, an extension of the shift makes it possible to obtain timber with better anatomical features.

**Conclusions**

As economic-environmental aspects are incorporated into the estimation of the forest shifts for *Eucalyptus grandis*, the optimal felling age increases.

The estimation of forest shifts for *E. grandis* is shown to involve a maximum average production, a Faustmann shift, a Hotelling shift, a Hartman shift and a maximum total production.

The Hartman shift is suitable for sustainable forest harvesting, inasmuch as it incorporates aspects of the proposal of Faustmann as well as the value of the environmental and recreational services provided by the plantation.

The extension of the forest shifts increases the volume of biomass, with the possibility of harvesting larger quantities of heartwood for cellulose and capturing more carbon, whereby the social benefit is enhanced.
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Conflict of interests

The authors declare they have no conflict of interests.

Contribution by author

Elizabeth Trujillo-Ubaldo: data analysis and interpretation, drafting of the introduction, results, discussion and conclusions sections of the manuscript; Plácido Salomón Álvarez-López: field work, drafting of the introduction, results, discussion and conclusions sections of the manuscript; Víctor Rafael Valdovinos Chávez: drafting of the introduction and results sections of the manuscript, general revision and editing; Gaudencio Benítez Molina: support in the drafting of the results, discussion sections of the manuscript, revision and editing; Luz Orieta Rodríguez: drafting of the abstract and introduction of the manuscript, general revision, design of figures and maps.

Referencias


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